

SLAC Summer Institute 2002
HF @ Tevatron

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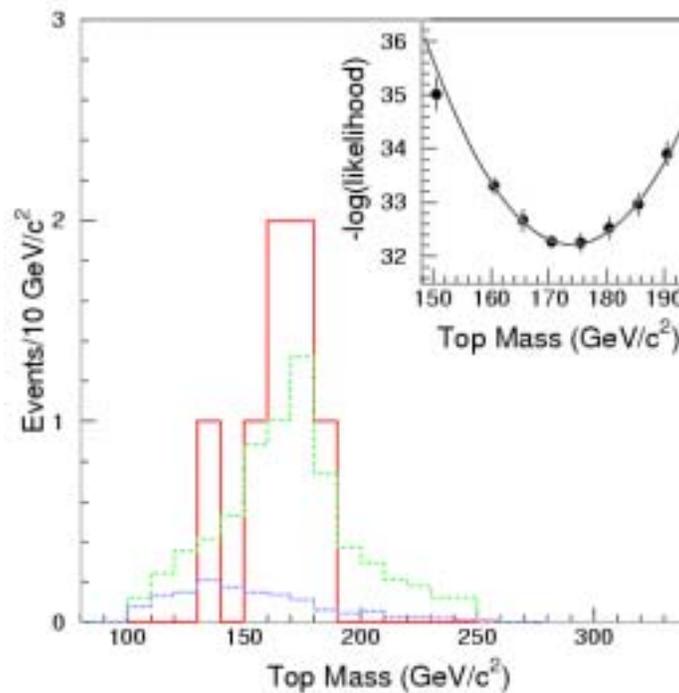
MIT/CDF

Discovering anything virtual

Overview of Lecture 3

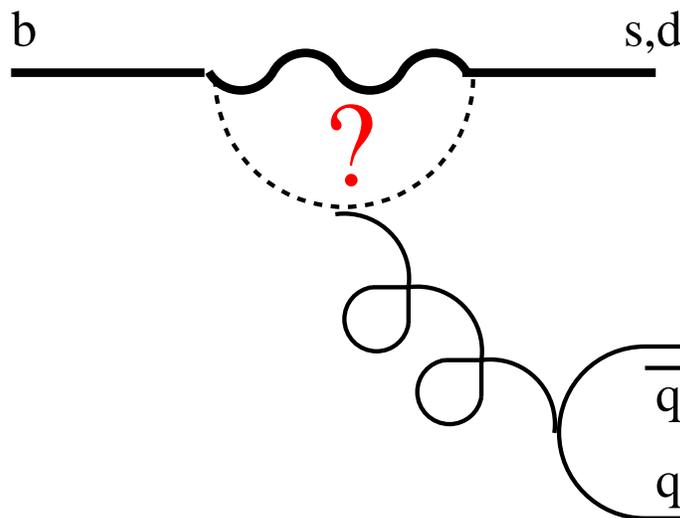
- New Physics vs Old Physics
⇒ *B* decays as a probe for the **Unknown**
- B_s mixing @ CDF
- Measuring γ @ CDF
- Measuring CP viol. phase of a penguin

New Physics via Observation of New Particle



→ Highest energies, low precision

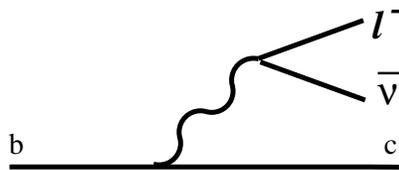
New Physics via Virtual Intermediate States



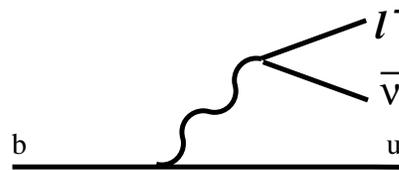
→ Highest precision, low energy

Impact of New Physics in B Decays

(Largely) independent of NP:

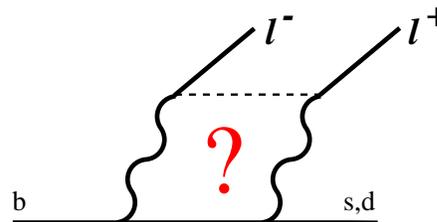
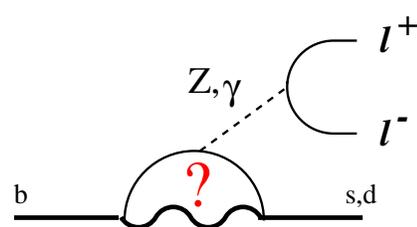
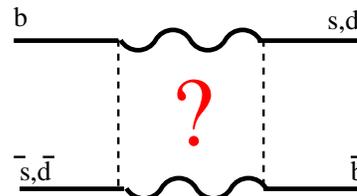
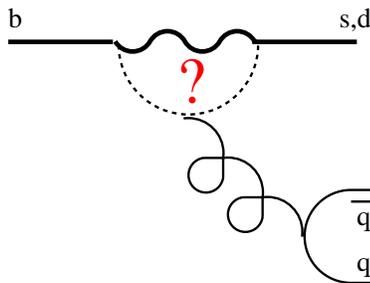


$|V_{cb}|$



$|V_{ub}| e^{i\gamma}$

Strikingly sensitive to NP:



Excellent Review of NP effects: Y.Nir hep-ph/9911321
e.g. SUSY, LR-symmetry, Multi-Higgs, new fermions, etc.

Rehash of CKM Matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_x c_z & s_x c_z & s_z e^{-i\phi} \\ -s_x c_y - c_x s_y s_z e^{i\phi} & c_x c_y - s_x s_y s_z e^{i\phi} & s_y c_z \\ s_x s_y - c_x c_y s_z e^{i\phi} & -c_x s_y - s_x c_y s_z e^{i\phi} & c_y c_z \end{pmatrix}$$

Subscript x, y, z are the three Euler angles.

s, c stands for sin, cos.

$$s_x = \lambda, \quad s_y = A\lambda^2, \quad s_z = O(\lambda^3) \quad \lambda = 0.22, \quad A = 0.8$$

Phase shows up at $O(\lambda^3), O(\lambda^4), O(\lambda^5), O(\lambda^6)$

Guiding principle for phase convention:

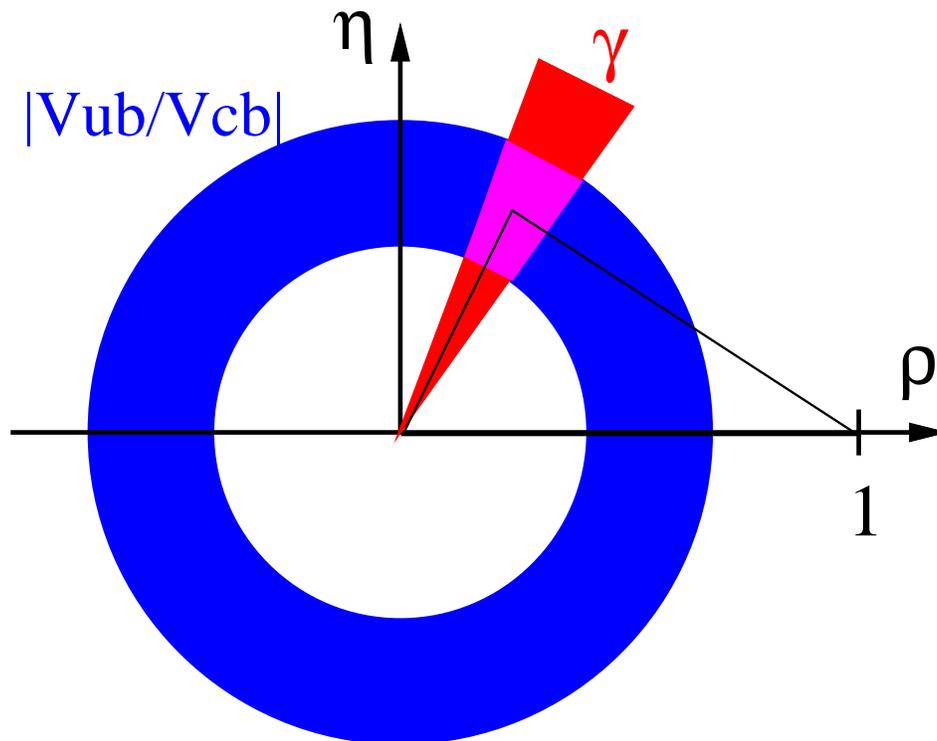
Dominant processes are chosen to have zero phase !

Note: KM originally chose convention that gives zero phase to first row and column.

B Decays within the SM

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & |V_{ub}| \times e^{-i\gamma} \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & |V_{cb}| \\ \lambda|V_{cb}| - |V_{ub}| \times e^{+i\gamma} & -|V_{cb}| & 1 \end{pmatrix} + O(\lambda^4)$$

Measurements free of New Physics in loops:



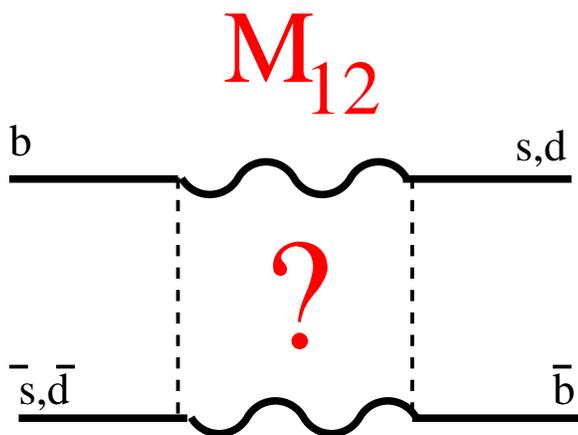
Roadmap towards anything Virtual

- Measure λ , $|V_{cb}|$, $|V_{ub}|$, γ in tree level processes.
- Use theory to predict loop processes.
- Measure loop processes and compare with theory predictions.

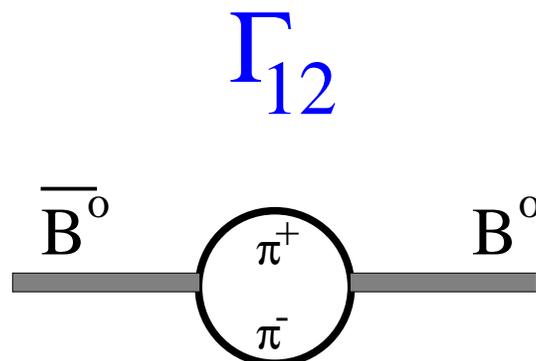
Example: Meson Mixing

$$i \frac{d}{dt} \begin{pmatrix} a \\ b \end{pmatrix} = (M - \frac{i}{2}\Gamma) \begin{pmatrix} a \\ b \end{pmatrix}$$

$$|B(t)\rangle = a|B^0\rangle + b|\bar{B}^0\rangle$$



off shell
intermediate state



on shell
intermediate state

$$|M_{12}| \gg |\Gamma_{12}|$$

Physical Observables in B_d Mixing

$$\begin{aligned} \Delta m &= 2|M_{12}| \\ \Delta\Gamma &= 2\text{Re}(M_{12}\Gamma_{12}^*)/|M_{12}| \quad \propto \cos 2\beta \\ A_{cp}^{mix}(t) &= \pm \text{Im}\left(\frac{M_{12}^*\bar{A}}{|M_{12}|A}\right) \times \sin \Delta mt \quad \propto \sin 2(\beta + \theta) \end{aligned}$$

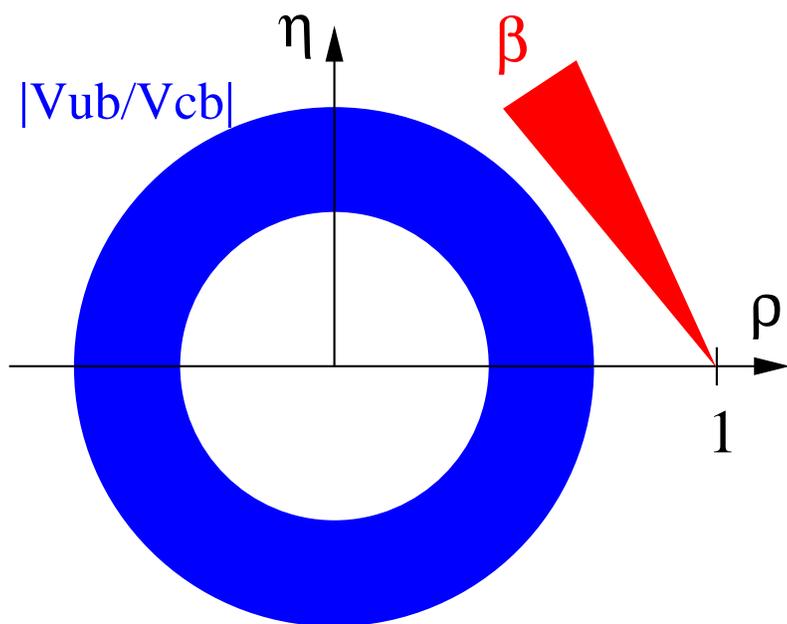
$$2\beta \quad := \quad \text{Arg}(M_{12})$$

$$2\theta \quad := \quad \text{Arg}\left(\frac{\bar{A}}{A}\right)$$

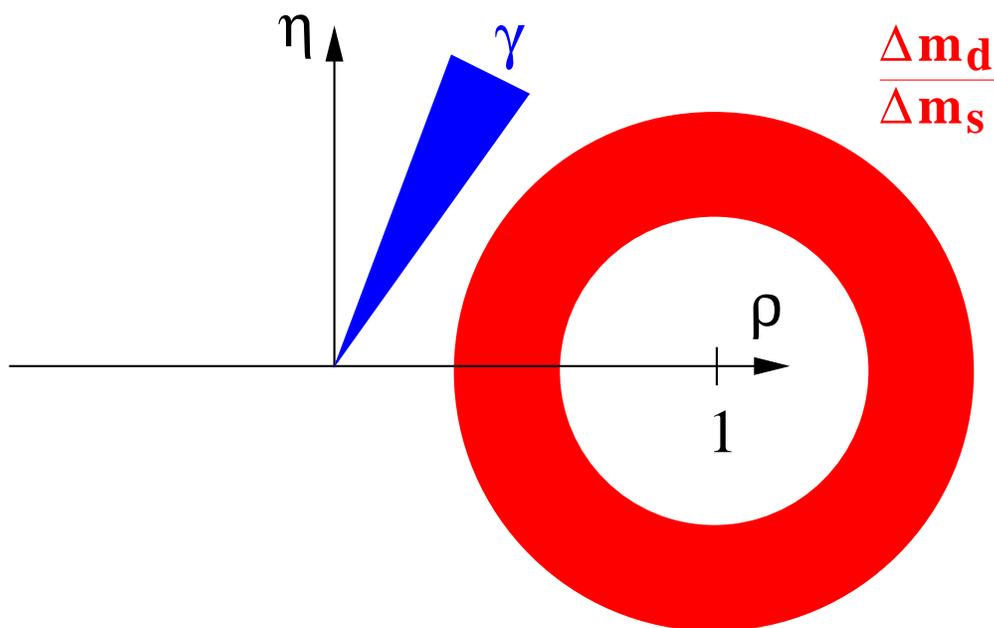
$$b \rightarrow c \quad \rightarrow \quad \theta = 0 \quad \text{by definition}$$

$$b \rightarrow u \quad \rightarrow \quad \theta = \gamma$$

We measure β via $A_{cp}^{mix}(t)$ in $b \rightarrow c$ and γ via comparison with $A_{cp}^{mix}(t)$ in $b \rightarrow u$.

Observing New Physics in M_{12} 

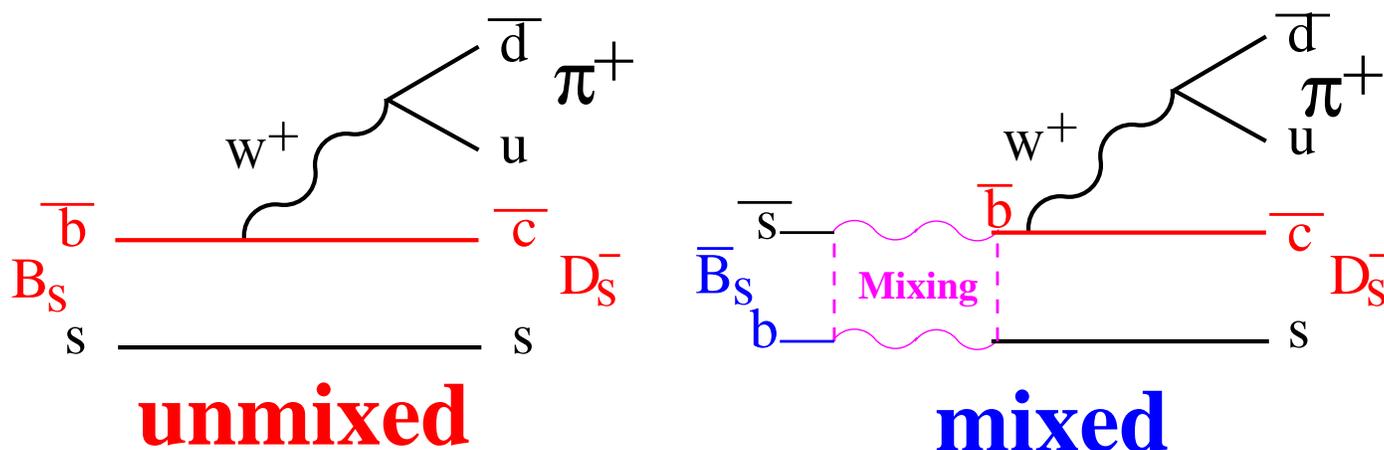
**CP violating
New Physics
in mixing**



**CP conserving
New Physics
in mixing**

B_s Mixing

Measuring B_s mixing



- Trigger on & reconstruct the signal
- suppress bkg
- measure the flavor @ production
- measure flight distance
- measure B_s momentum

Meson Mixing

$$\begin{aligned}
 A_{mix} &= \frac{N_{unmixed} - N_{mixed}}{N_{unmixed} + N_{mixed}} \\
 &= D \cos \Delta m t
 \end{aligned}$$

$$D = 2P_{tag} - 1$$

$$Sig(\Delta m) = \sqrt{\frac{N\epsilon D^2}{2}} e^{-(\Delta m \sigma_t)^2/2} \sqrt{\frac{S}{S+bkg}}$$

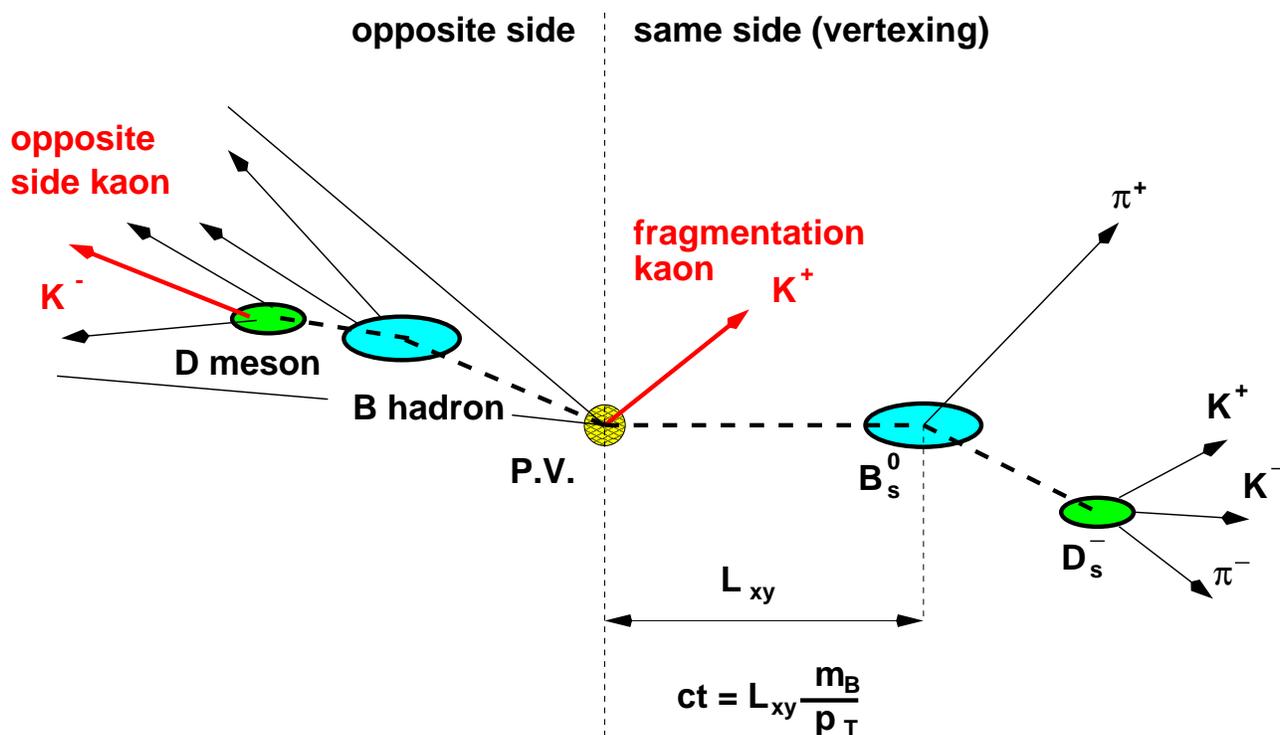
Note: $\Delta m \sigma_t < 1$ for $\Delta m/\Gamma < 33(25)$ with(without) L00

Trigger & reconstruct the Signal

$B_s \rightarrow D_s^\pm \pi^\mp$	$D_s \rightarrow \phi\pi$	16k
	$D_s \rightarrow K^{*0}K^-$	15k
	$D_s \rightarrow \pi^+\pi^-\pi^+$	5.5k
<hr/>		
$B_s \rightarrow D_s^\pm \pi^\mp$	<i>all</i>	37k
<hr/>		
$B_s \rightarrow D_s^\pm \pi^+\pi^-\pi^\mp$	$D_s \rightarrow \phi\pi$	15k
	$D_s \rightarrow K^{*0}K^-$	17k
	$D_s \rightarrow \pi^+\pi^-\pi^+$	6k
<hr/>		
$B_s \rightarrow D_s^\pm \pi^+\pi^-\pi^\mp$	<i>all</i>	38k

Note: This is official CDF PR. It includes only trigger & tracking acceptance.

Flavor Tagging at CDF



	Run1	Run2
Same-Side	1.0	4.2
Soft Lepton	1.7	1.7
Jet Charge	3.0	3.0
Opposite Kaon	0.0	2.4
Total	5.7	11.3

Table 1: ϵD^2 in % , Fermilab Proposal 909, 1998.

$\Upsilon(4s)$ vs Hadron Collider

$\Upsilon(4s)$

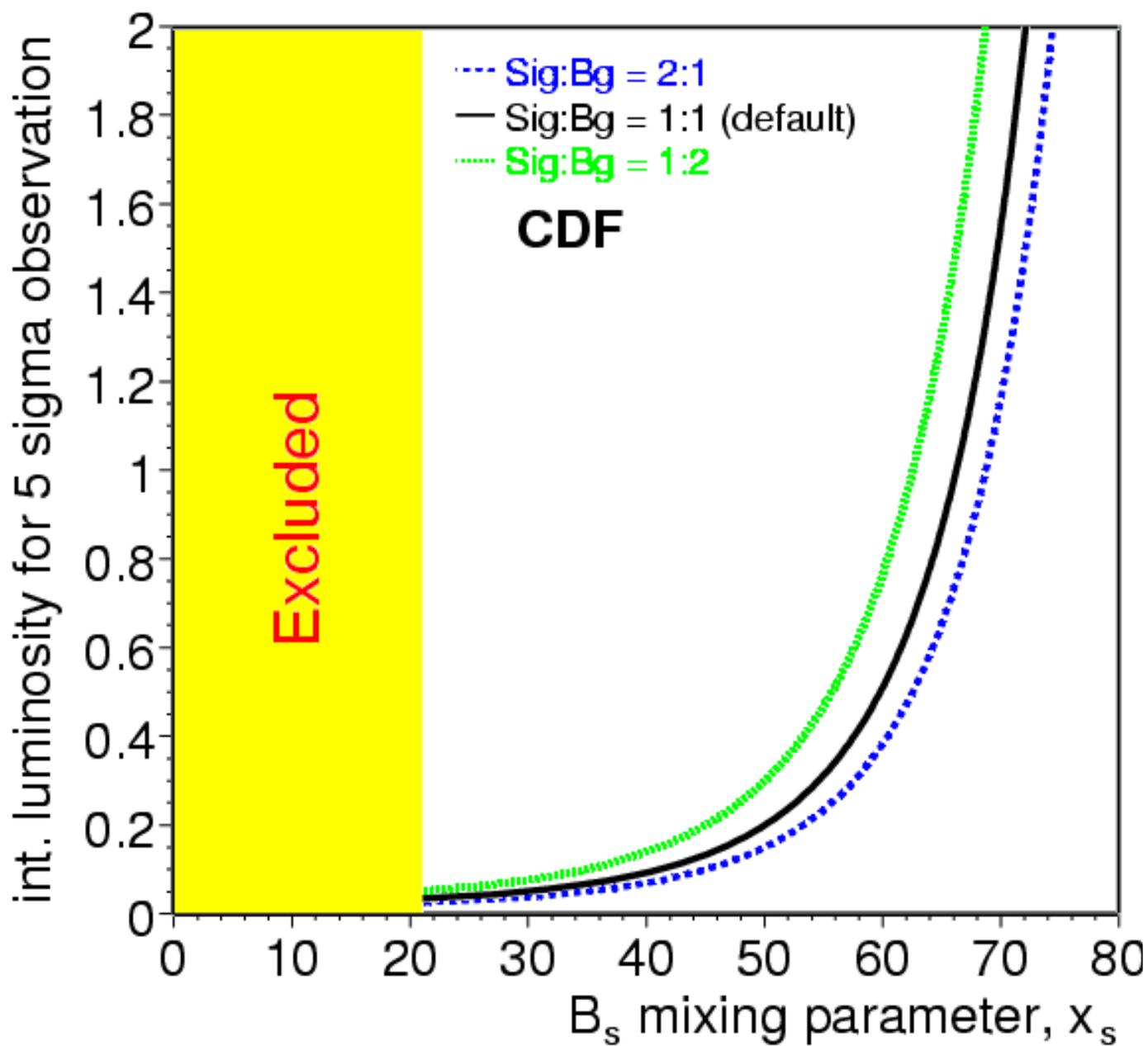
- coherent $B^0 - \overline{B}^0$ production.
 \Rightarrow the other b -quark ALWAYS tags the flavor.
- Geometric Acceptance 95 – 98% of 4π .
 $\Rightarrow \epsilon D^2$ is large ($\sim 30\%$)

Hadron Colliders

- the other b -quark hadronizes as B^0, B^+, B_s, Λ_b , etc.
 $\Rightarrow D$ is decreased by mixing:

$$\begin{aligned}
 D_{max} &= 2P_{max} - 1 \\
 &= 2(1 - f_d \cdot \chi_d - f_s \chi_s) - 1 \\
 &\sim 0.7
 \end{aligned}$$

- Geometric Acceptance is far from complete because of production characteristics.
- inferior Kaon particle ID

PR: Mixing Reach in Hadronic Decays

“Conservative” Perspective

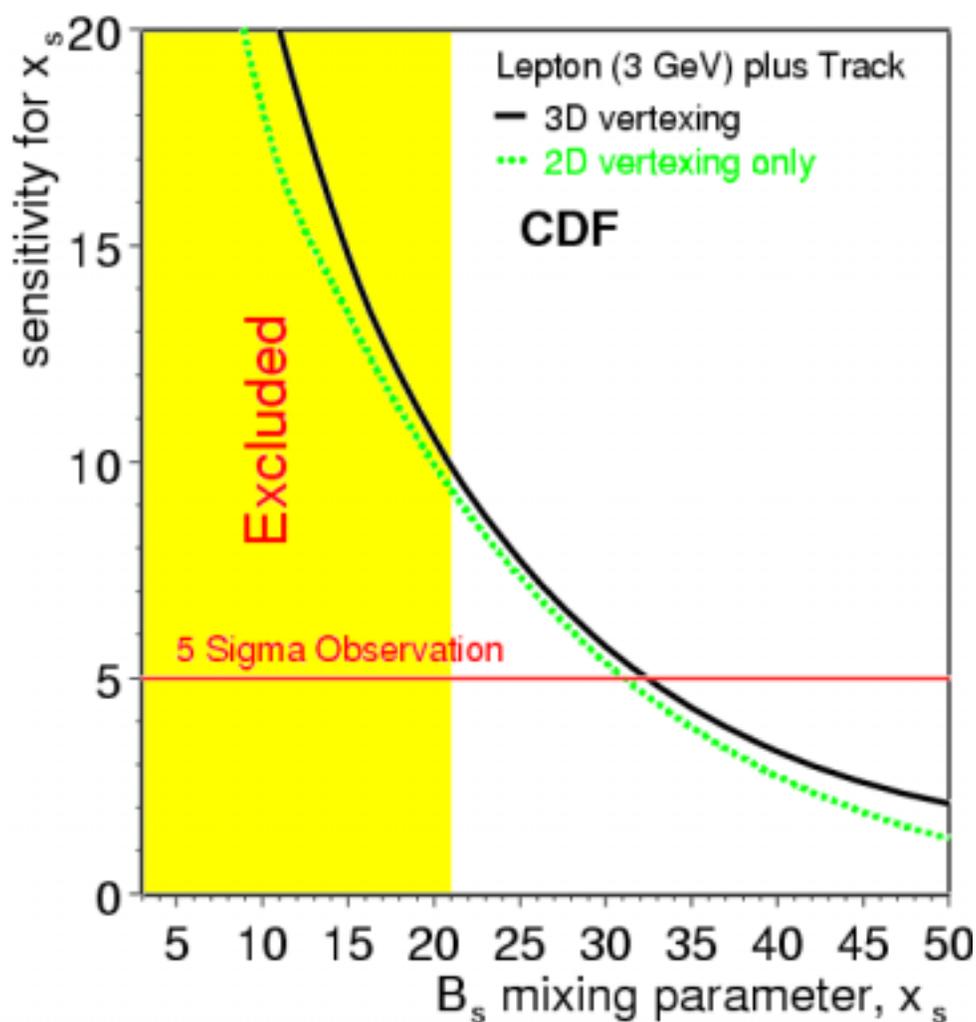
Analysis cuts	×	2
$B_s \rightarrow D_s \pi$ only	×	2
no L00	×	1.5 @ $x_s = 25$
svx & svt ineff.	×	2.4
Run1 ϵD^2	×	2.0

Take your pick on these factors and multiply y-axis on previous page by it to arrive at **your own** best guess as to how mu8ch lumi is required to measure x_s .

Aside: Mixing via semi-leptonic decays

Proper time resolution

$$\begin{aligned}
 ct &= \frac{L_{xy} m_{B_s}}{p_T(lD_s)} \times \kappa \\
 \sigma_t &= \sqrt{\sigma_{t0}^2 + \left(t \frac{\sigma_\kappa}{\kappa}\right)^2} \\
 &\sim \sqrt{(60 \text{ fs})^2 + (0.14 t)^2}
 \end{aligned}$$



Measuring γ

Measuring γ — the principle

$$\begin{aligned}\gamma &= \text{Arg}(V_{ub}^* V_{ud} V_{cb} V_{cd}^*) \\ &= \text{Arg}(V_{ub}^*) + O(\lambda^5) \text{ (standard phase conv.)}\end{aligned}$$

BTeV expectations: $B_s \rightarrow D_s K, B_d \rightarrow DK$ results in $\sigma_\gamma \sim 5 - 10^\circ$ after two years of running, i.e. $\sim 2008 - 2010$.

Measuring γ is very difficult !!!

Fertile ground for new ideas !!!

Measuring γ — an alternative approach

If Penguins didn't exist:

$$\text{Im}\left(\frac{\bar{A}M_{12}^*}{A|M_{12}|}\right)$$

$$B_d \rightarrow \pi^+ \pi^- \quad \sin 2(\gamma + \beta)$$

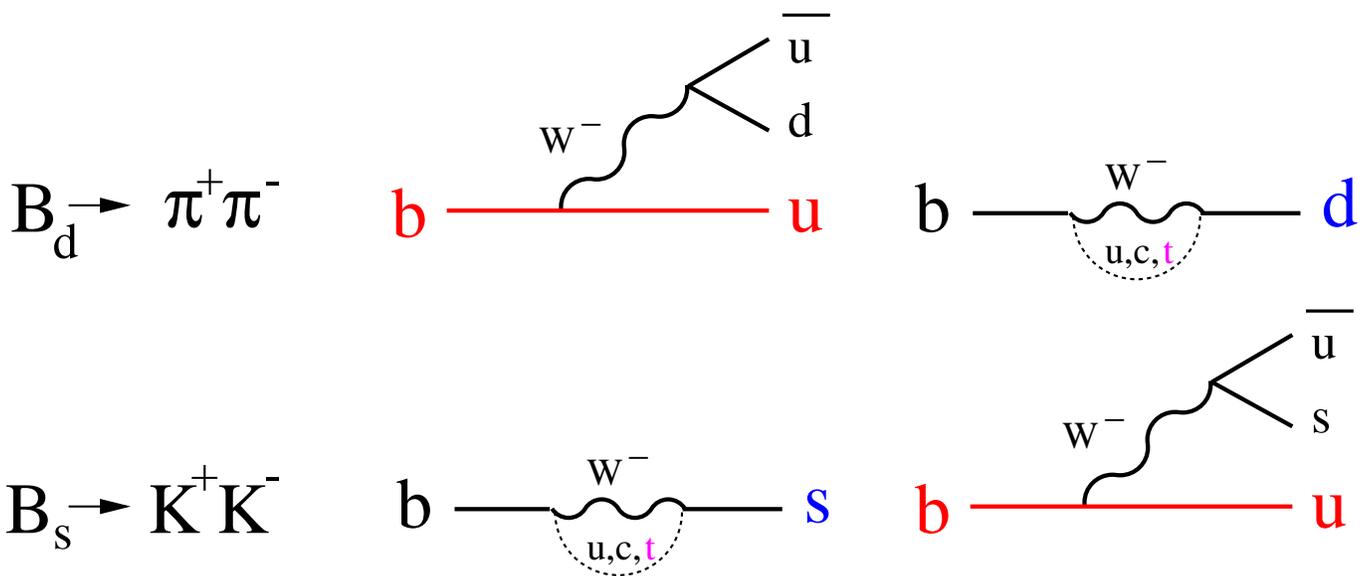
$$B_d \rightarrow J/\psi K_s \quad \sin 2\beta$$

but nature's not this simple ...

“Penguin Pollution”

Dominant

Subdominant



$$\frac{\text{Subdominant}}{\text{Dominant}} \sim 0.2 - 0.4$$

Penguin cleanup by relating CP asymmetries in $B_d \rightarrow \pi^+ \pi^-$ to $B_s \rightarrow K^+ K^-$ via SU(3) flavor.

Measuring γ @ CDF

CP Violation in $B_d \rightarrow \pi^+ \pi^-$, $B_s \rightarrow K^+ K^-$

$$A_{CP}(t) = A_{dir} \cos \Delta mt + A_{mix} \sin \Delta mt$$

Combined fit to $B_d \rightarrow \pi^+ \pi^-$, $B_s \rightarrow K^+ K^-$

- Measure $A_{dir}^{\pi\pi}$, $A_{mix}^{\pi\pi}$, A_{dir}^{KK} , A_{mix}^{KK} .
- UT triangle fixes β
- **extract weak phase γ**
- **extract strong phase and modulus of penguin/tree ratio**

Aside: Details in Tevatron Run II B-workshop write-up.

Measuring γ — the details

(R.Fleischer PLB459 (1999) 306)

χ^2 fit to 5 experimental results

Four unknowns:

- d = ratio of hadronic matrix elements " P/T " ~ 0.3
- θ = strong phase of ratio of hadronic matrix elements $\sim 0???$
- γ, β = weak phases

Five observables:

$$A_{cp}(t) = A_{cp}^{dir} \times \cos \Delta mt + A_{cp}^{mix} \times \sin \Delta mt$$

$$A_{cp}^{dir}(\pi^+\pi^-) = -2d \sin \theta \sin \gamma + O(d^2)$$

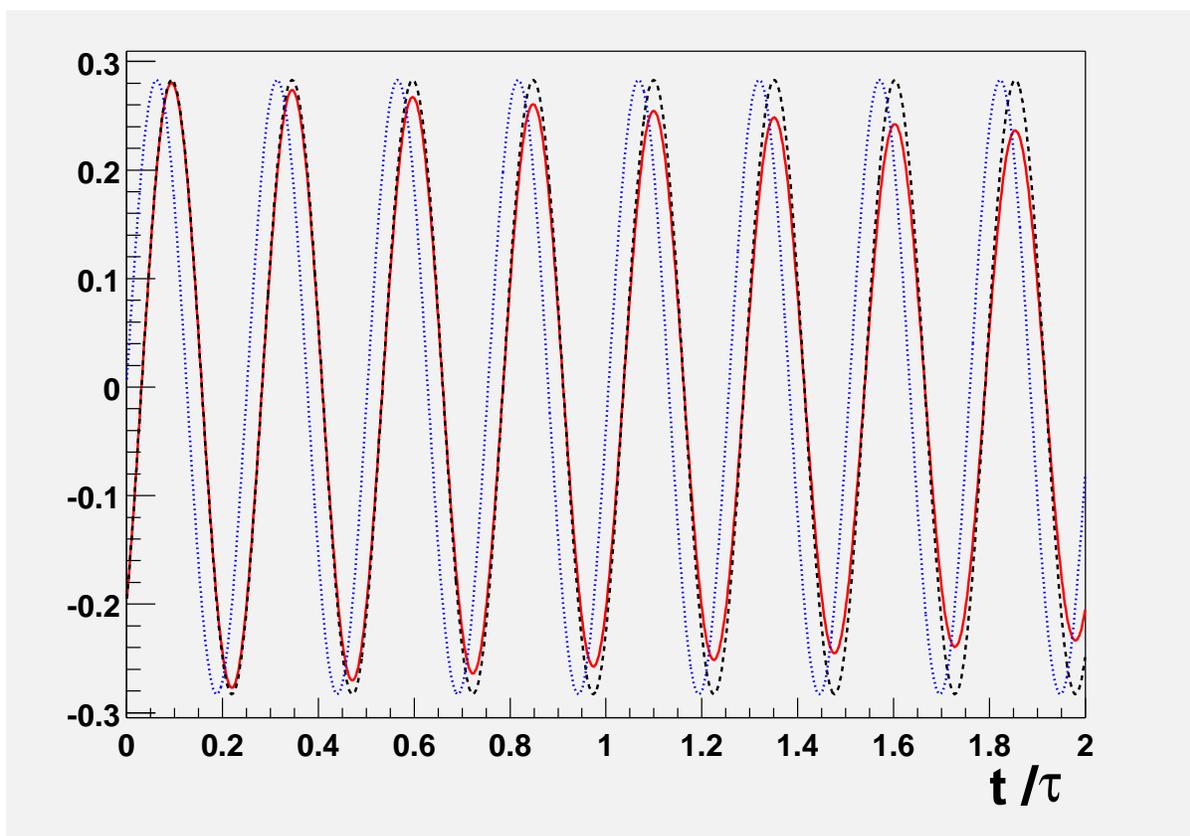
$$A_{cp}^{dir}(K^+K^-) = \frac{2\lambda^2}{d(1-\lambda^2)} \sin \theta \sin \gamma + O\left(\left(\frac{\lambda^2}{d}\right)^2\right)$$

$$A_{cp}^{mix}(K^+K^-) = \frac{2\lambda^2}{d(1-\lambda^2)} \cos \theta \sin \gamma + O\left(\left(\frac{\lambda^2}{d}\right)^2\right)$$

$$A_{cp}^{mix}(\pi^+\pi^-) = \sin 2(\beta + \gamma) + 2d \cos \theta \times \\ (\cos \gamma \sin 2(\beta + \gamma) - \sin(2\beta + \gamma)) + O(d^2)$$

$$A_{cp}^{mix}(J/\psi K_s) = \sin 2\beta$$

CP Violation in $B_s \rightarrow K^+ K^-$



blue: $A_{dir} = \Delta\Gamma = 0$

black: $\Delta\Gamma = 0$

red: $A_{dir}, A_{mix}, \Delta\Gamma$ non-zero

$$\frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}} = \frac{2e^{-\langle\Gamma\rangle t}}{e^{-\Gamma_H t} + e^{-\Gamma_L t} + A_{\Delta\Gamma}(e^{-\Gamma_H t} - e^{-\Gamma_L t})} \times (A_{mix} \sin(\Delta mt) + A_{dir} \cos(\Delta mt))$$

Yields and Expected errors

Assume **SU(3)** and B_d/B_s production ~ 2.5

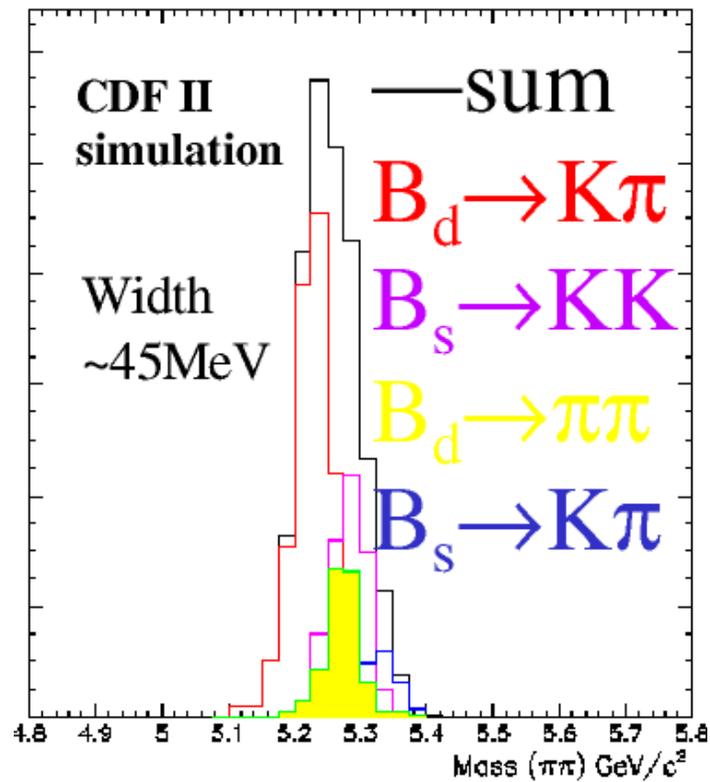
$B_d \rightarrow \pi^+ \pi^-$	$B_d \rightarrow K^+ \pi^-$	$B_s \rightarrow \pi^+ K^-$	$B_s \rightarrow K^+ K^-$
1	4	0.5	2
5-10k	20-40k	2.5-5k	10-20k

Experimental Errors for “nominal assumptions”:

$$\sigma_{Acp} \sim 0.08 \text{ for } B_s \rightarrow K^+ K^-$$

$$\sigma_{Acp} \sim 0.14 \text{ for } B_d \rightarrow \pi^+ \pi^-$$

Distinguishing $\pi\pi, K\pi, KK$

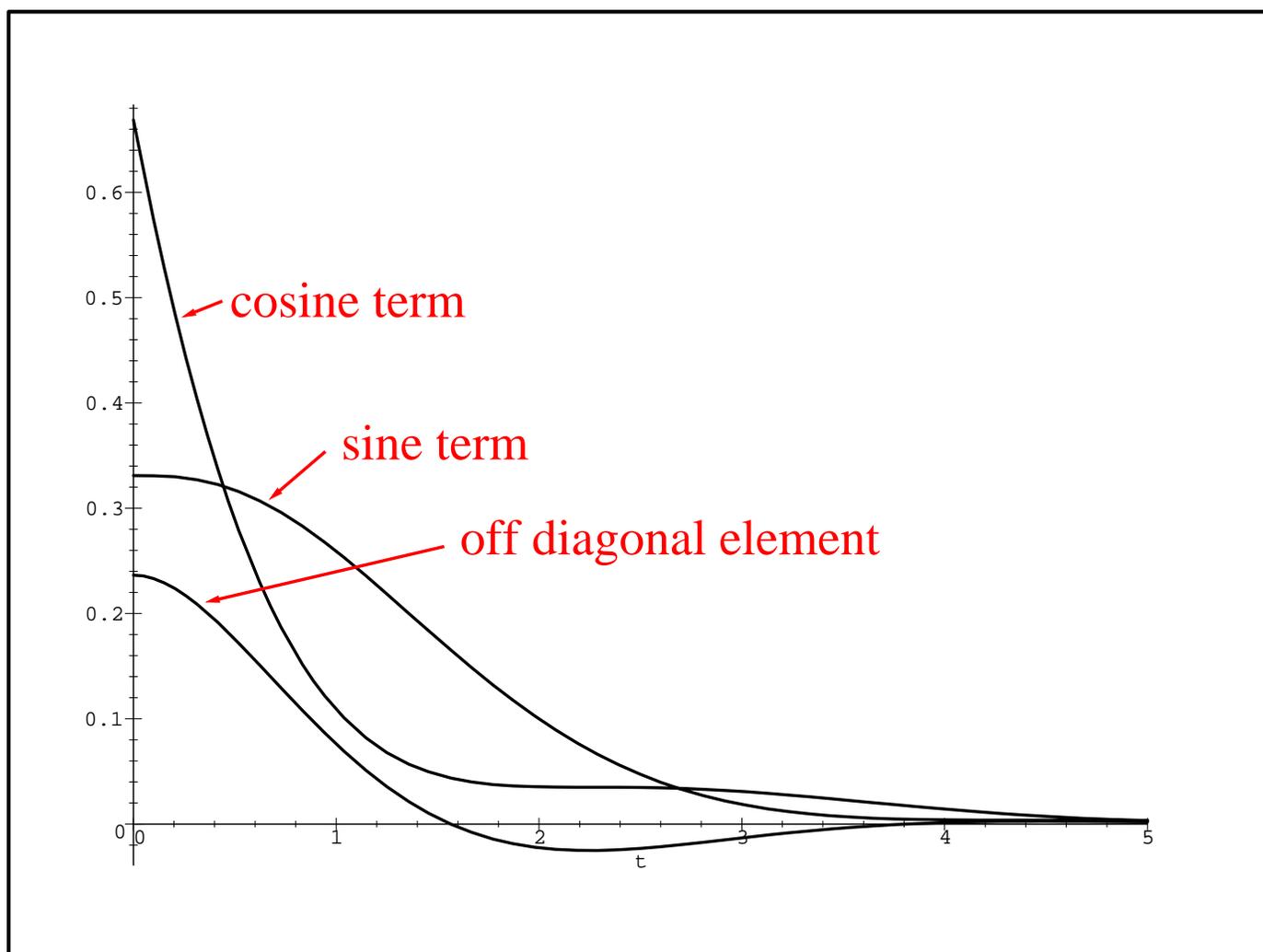


	$K\pi$	$\pi\pi$	KK
B_d	20k	5k	0
σ	0.95%	2.8%	-
B_s	2.5k	0	10k
σ	4.8%	-	1.6%
bkg	14k	28k	14k
	“Effective” S/bkg		
B_s :	0.21	-	0.64
B_d :	1.24	0.34	-

Sensitivity for A_{cp} — analytical expressions

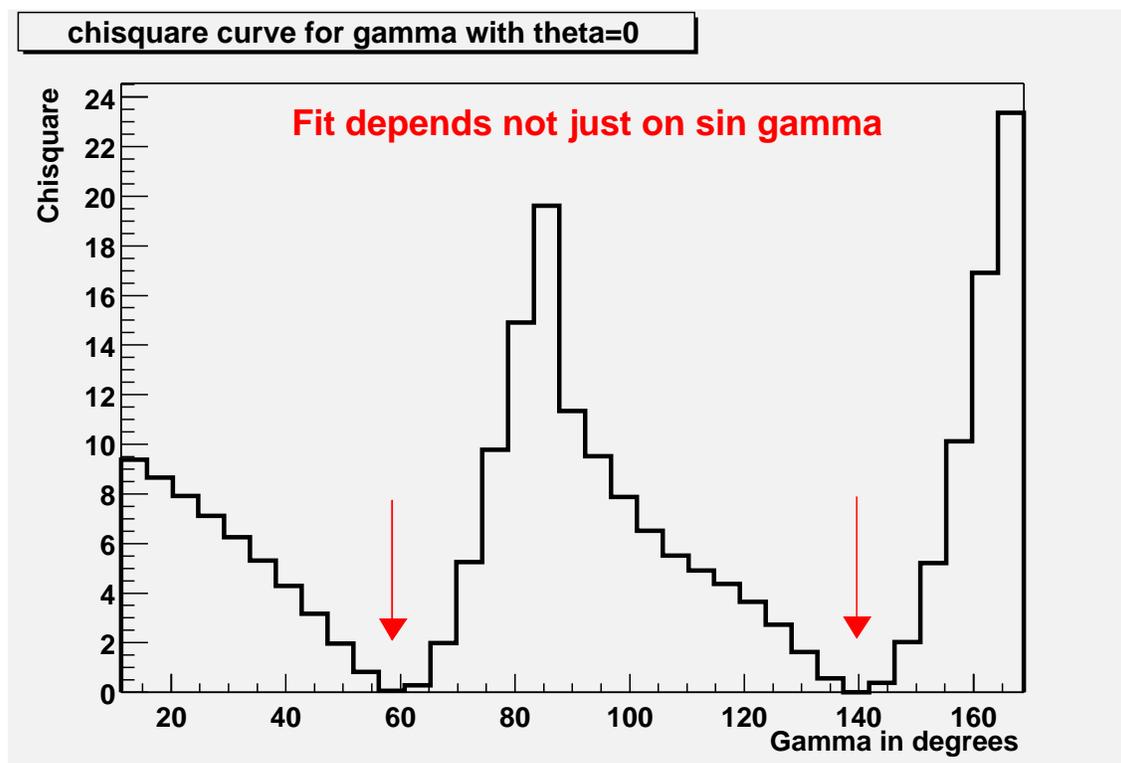
$$A_{cp} = A_{cp}^{dir} \times \cos xt + A_{cp}^{mix} \times \sin xt$$

G = inverse of cov. matrix for A_{cp}^{dir} , A_{cp}^{mix}



Expected Reach in Run IIa

χ^2 fit for γ :



$$\sigma_\gamma = {}^{+5.4}_{-6.8} \pm 3 \text{ degrees}$$

Systematic Error due to SU(3) breaking of 20%:
 $\sim 1/2$ the expected experimental error !!!

Aside: Comparable to BTeV reach in $B_s \rightarrow D_s K$ by 2008-2010.

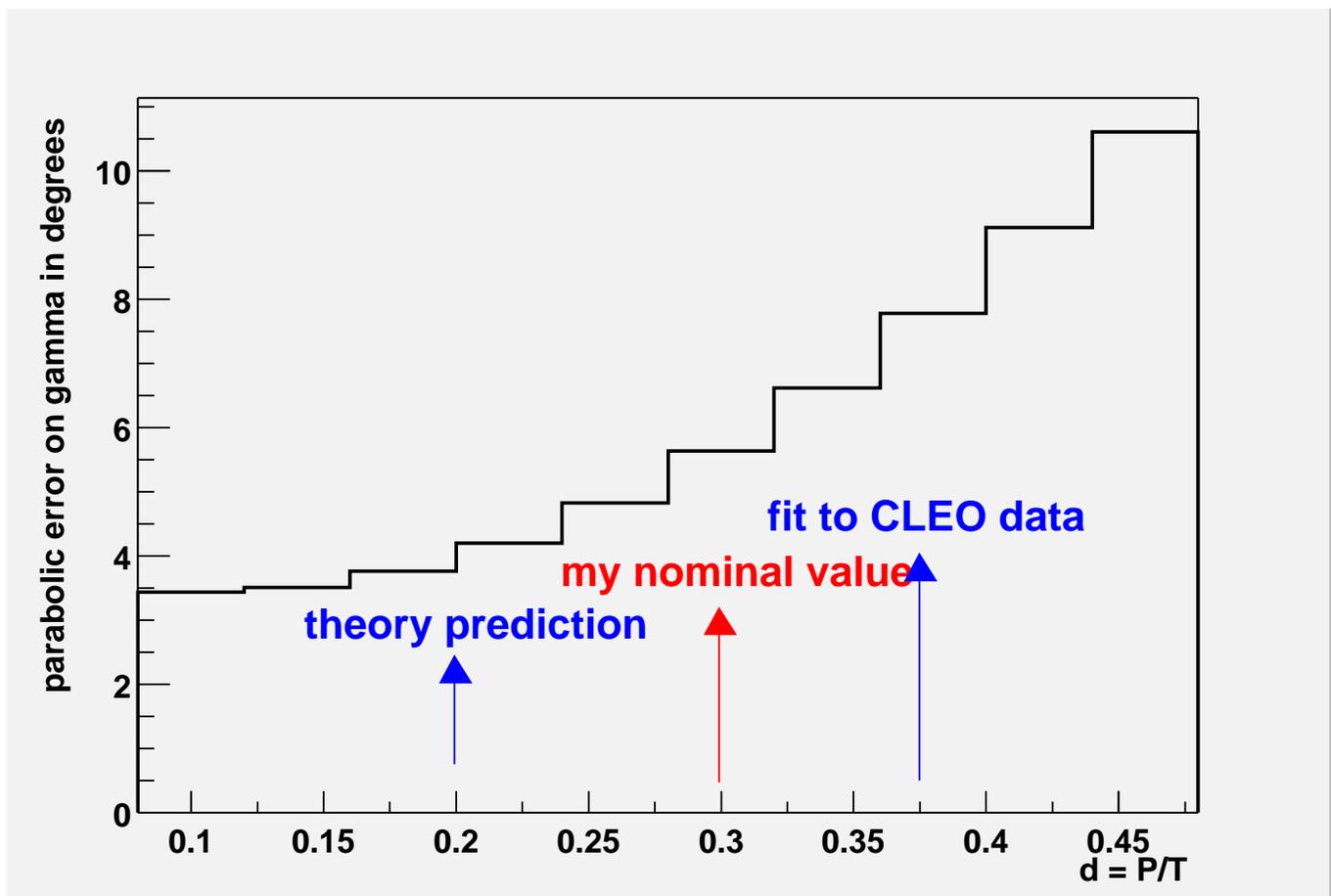
A word about theory systematics ...

- $B_d \rightarrow \pi^+ \pi^-$ measures $\sin 2(\beta + \gamma)$ up to $\sim 30\%$ “penguin pollution”.
- “penguin pollution” cleaned up by $B_s \rightarrow K^+ K^-$ up to $\sim 20\%$ SU(3) breaking.

SU(3) symmetry breaking is a “2nd order” effect on the measurement of γ .

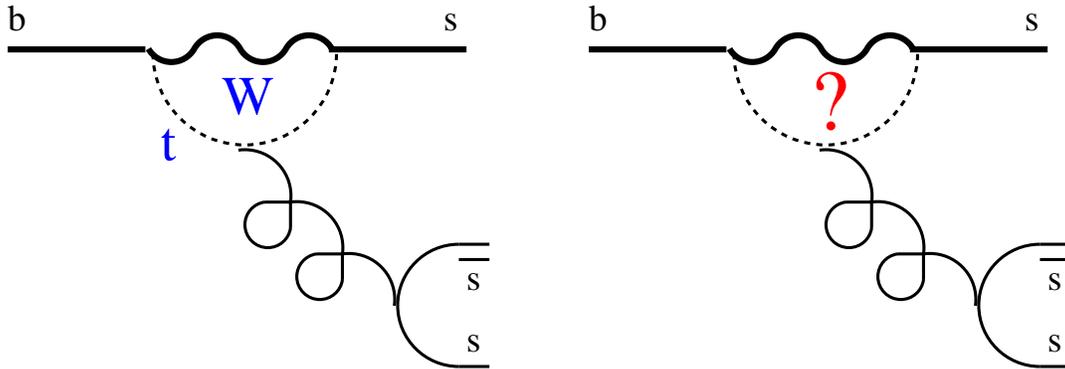
Aside: SU(3) breaking tends to cancel in rate ratios like CP asymmetries. To be conservative, we ignored this fact.

Dependence on “Nature’s choice”



Large Penguin Correction to untangle \Leftrightarrow Large error on γ

Chasing SUSY with Penguins



$$A_{SM} \propto \lambda^2 \frac{\alpha_s}{4\pi}$$

$$A_{NP} \propto \frac{M_W^2}{M_{NP}^2}$$

$$\frac{A_{NP}}{A_{SM}} \sim O(1) \Leftrightarrow M_{NP} \sim 3 \text{ TeV}$$

SUSY may lead to $A_{CP}(B^\pm \rightarrow \phi K^\pm) \sim 30\%$ (PRD63 (2001) 015003)

Expect 1.4 – 1.9k events @ BR=5.5e-6
($\sim 1000 \text{ fb}^{-1}$ @ $\Upsilon(4S)$)

$> 4\sigma$ “observation” up to S/bkg $\sim 1/4$

Other beautiful Physics

- $\Delta\Gamma$ & $Arg(M_{12})$ using $B_s \rightarrow J/\psi\phi$; CDF(BTeV) expects 4000(20,000) events/ 2fb^{-1}
- Measure $\beta + \gamma$ using $B_d \rightarrow \pi^+\pi^-\pi^0$; BTeV expect $\epsilon D^2 \times \text{yield} = 500$ events.

3 Lectures Conclusion

- D0 & CDF Run2 physics program are finally starting.
- Likely to start being competitive with BaBelle by Summer 2003 on a number of charm- and B-physics topics.
- Unique opportunities: $\Delta m_s, \gamma$